

1. Implement IB method with different discrete Delta functions for 1D interface problems with a true solution. Do the grid refinement analysis for the following.
 - (a) Check the local truncation error. Find the order of discretization at regular grid points and irregular grid points.
 - (b) Check the global error. Find the order of convergence.
 - (c) Plot the true and finite difference solution in one plot for $n = 40$ and $n = 80$ and the error plot as well.
 - (d) Plot the error versus the step size h using the log – log plot.
 - (e) Numerically check the moment equations for different discrete Delta functions.
 - (f) Let the interval be $[0, 1]$ and $f(x, t) = \delta(x - 1/3) * \exp(-t)$, and $\alpha(0) = 1/3$, and $d\alpha/dt = u(\alpha)$, numerically tracking the interface α and the solution.